

Electrostatic Zipping Actuators and Their Application to MEMS

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01/15/2004

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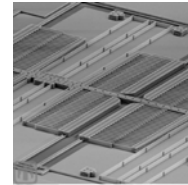


Introduction



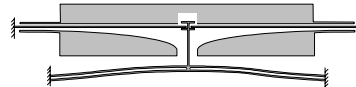
Problem

- Need powerful electrostatic actuators for MEMS power relay
- Huge size using conventional designs

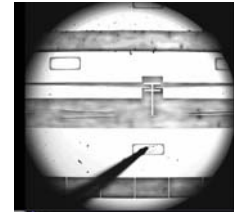
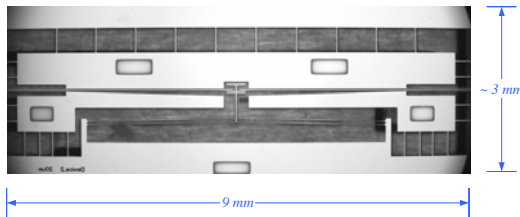


Solutions

- Zipping actuator with compliant starting zone



Results



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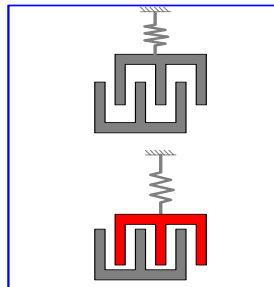
Contributions



- Design: Starting zone to reduce the pull-in voltage
- Numerical and analytical modeling: easy and accurate
- Optimization of the system
- Specified design for implementation in a relay
- Fabrication and measurement of the actuator-relay
- Wet-anisotropically-etched micro relay contact

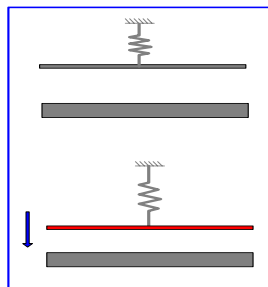
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Background: Electrostatic Actuators



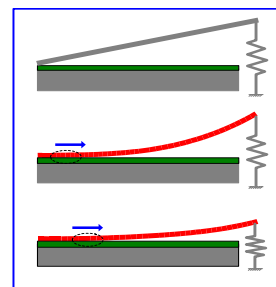
▪ Comb Drive

- Force independent of stroke: large stroke
- Very small force, large deflection



▪ Parallel Plate

- Conflition between stroke and force



▪ “Zipper”

- Large force and large deflection
- High voltage for pull_in

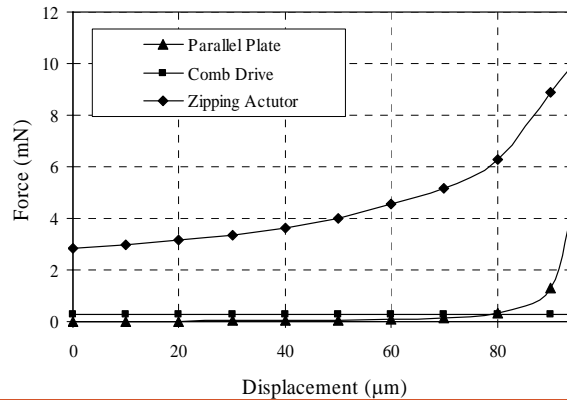
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F-D Curve of Three Electrostatic Actuators



Force-Displacement Character of the three actuators

- With the same volume and same voltage, the “zipper” actuator achieves a much larger force than comb drive and capacitor plate actuators
- “Zipper” actuator is the only hope to secure milli Newtons of force with a reasonable volume



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Zippering Actuators: A Survey



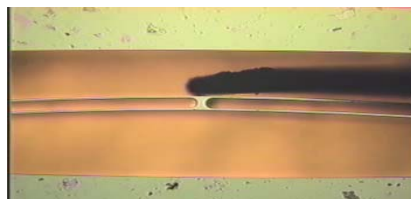
Author	Actuation direction	Application	Size (mm^2)	Force (mN)	Stroke (μm)
Shikida	Vertical	Valve	5 * 5	N/A (very small)	220
Divoux	Vertical	Mirror	0.8 * 0.8	0.1	6
Legtenberg	Lateral	N/A	0.8 * 0.5	0.02	30
Perregaux	Lateral	Optical shutter	0.5 * 0.2	N/A (very small)	20
Sherman	Lateral	Fluid control	1 * 0.2	N/A (very small)	100
This thesis	Lateral	Relay	9 * 1	2 ~ 10	80

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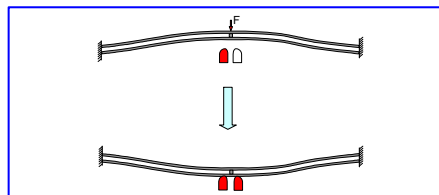
Example Load: Double Beam



- A pre-curved bistable MEMS mechanism
- Promising as a micro relay structure
 - Simple structure
 - No residual stress
 - High contact force: good for on-state performance
- Need an electrostatic actuator to make the MEMS relay



Double beam



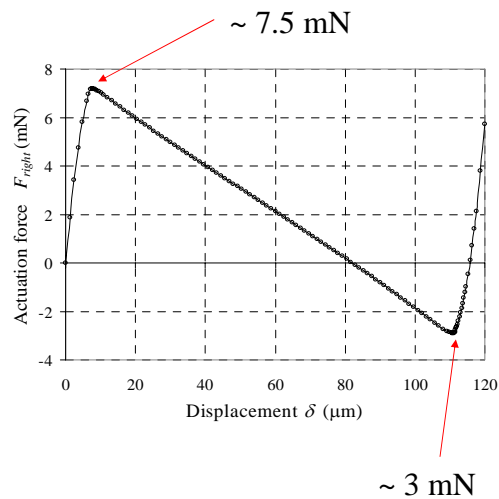
Double beam working as a Relay

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Why Is It Hard ? (1)



- Stroke: $\geq 80 \mu\text{m}$
- Asymmetric and high actuation/contact force: $\sim 7 \text{ mN}$ for the first $10 \mu\text{m}$ to get a 3 mN of contact force
- Actuation voltage: $< 200 \text{ V}$ (as small as possible)
- Scale: $7 \times 7 \times 1 \text{ mm}^3$
- Fabrication: Deep Reactive Ion Etching



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Why Is It Hard ? (2)

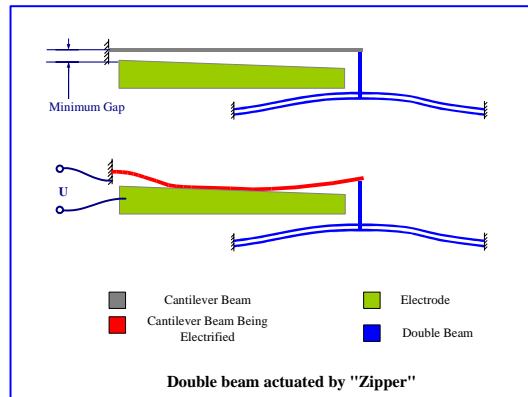


Initial Design:

- DRIE etch through
- Attach the cantilever beam to the double beam
- Apply voltage between electrode and the cantilever beam.

Problem:

- Minimum gap due to DRIE aspect ratio of $\sim 5\%$
- Very High pull-in voltage because of the gap, about 250 V for a $15\ \mu\text{m}$ thick and $4.5\ \text{mm}$ long zipping beam.



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Contributions



- *Design: Starting zone to reduce the pull-in voltage*
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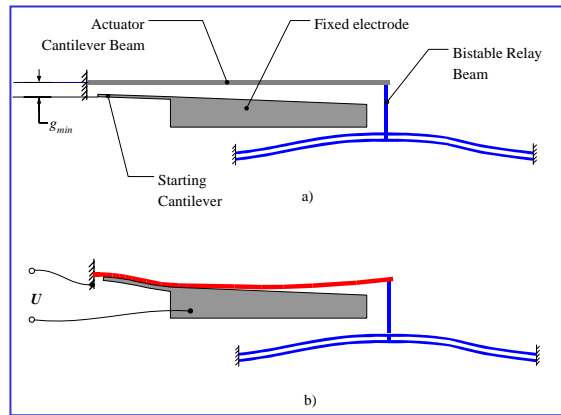
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Design: Compliant Starting Zone



- To reduce the pull-in voltage:

- A compliant starting zone
- Reciprocity: remove material not needed and not useful
- The starting zone bends up when voltage is applied between electrode and the beam
- The cantilever beam pulls-in and keep zipping at low voltage



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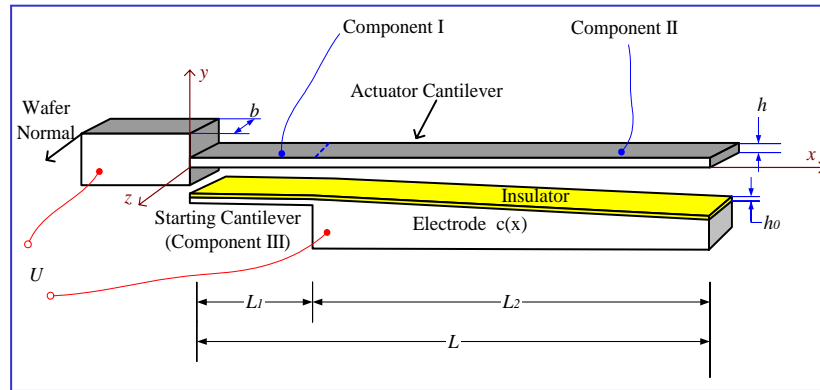
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Modeling: Overview



- Beam bending equation in electric field

$$E(I(x)y''(x))'' = \frac{-\epsilon_0 U^2 b}{2 \left[y(x) - c(x) + \frac{h_0}{\epsilon_r} \right]^2}$$

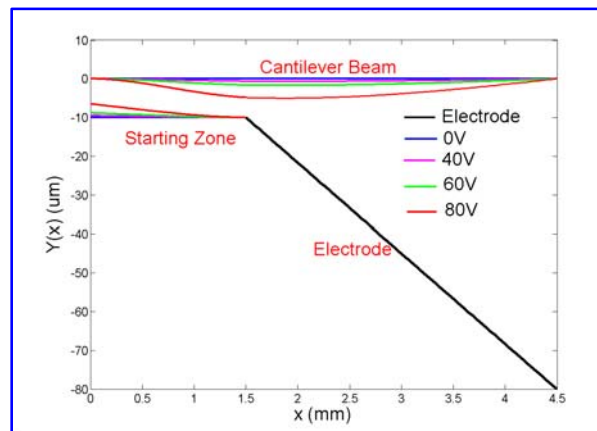
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Numerical Modeling: Before “Pull-in”



- Numerical Method

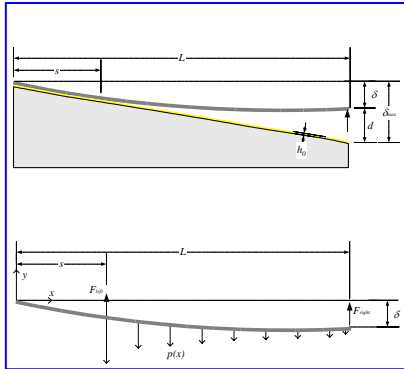
- Modeled as a device with Multiple-beams.
- Each beam is bent by the electrostatic force.
- The ODEs are solved simultaneously for each beam
- Deflection profiles for each beam are given out at different voltages.
- Actuation force can be calculated.
- Pull-in voltage can be found



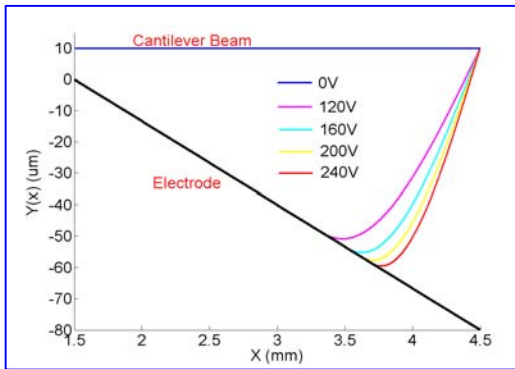
Deflection profiles of the cantilever beam and the starting beam at different voltages when the tip is constrained at zero displacement

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Numerical Modeling: After “Pull-in”



Model after pull-in



Cantilever Beam Deflection profiles when the tip is constrained at zero displacement (different voltages)

- Beam equation:
$$EIy''''(x) = p(x) = -\frac{\epsilon_0 b U^2}{2[y(x) - c(x) + h_0 / \epsilon_r]^2} \quad s \leq x \leq L$$

- Numerical solutions

- Eliminate varying B.C by adding parameter $\lambda = 1 - s/L$

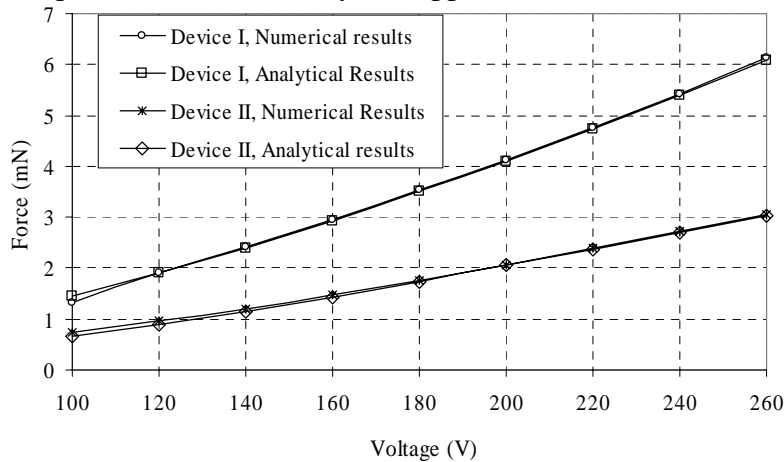
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Analytical Modeling: After Pull-in



- Approximation equation:
$$F_{right} \sim \frac{E^{1/4} b}{\sqrt{d}} \left(\frac{\epsilon_0 \epsilon_r U^2 h}{h_0} \right)^{3/4}$$

- Comparisons between analytical approximations and numerical results:



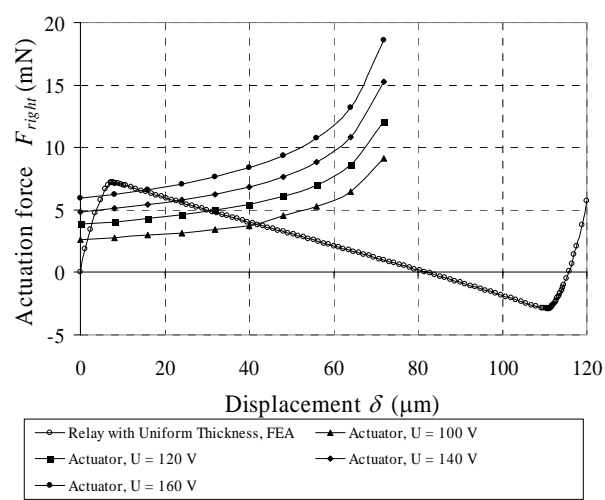
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Forces: Actuator vs. Switch Beam



- Force-Displacement curves of the actuator and the double beam

- > 160V is needed to actuate the double beam with ~ 3 mN of contact force
- Can we change the force-displacement curve of the double beam without reducing the contact force?



Force-Displacement curves of the actuator and the double beam

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Contributions



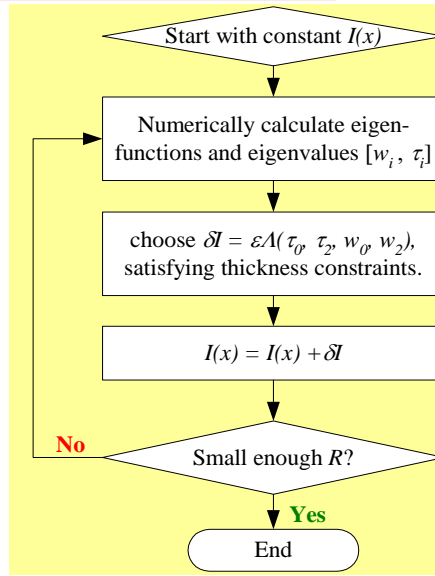
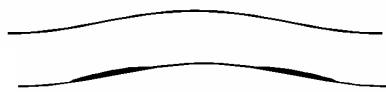
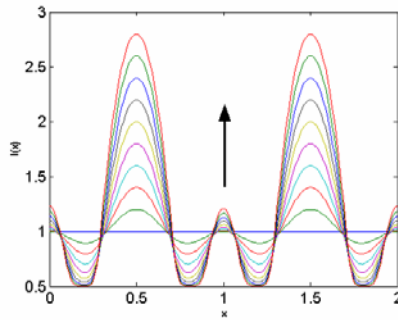
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Optimization of The Double Beam



- Force ratio $R = C(\tau_0, \tau_2)$
- $\delta C(\tau_0, \tau_2) = \int (\delta I) \Lambda(\tau_0, \tau_2, w_0, w_2)$

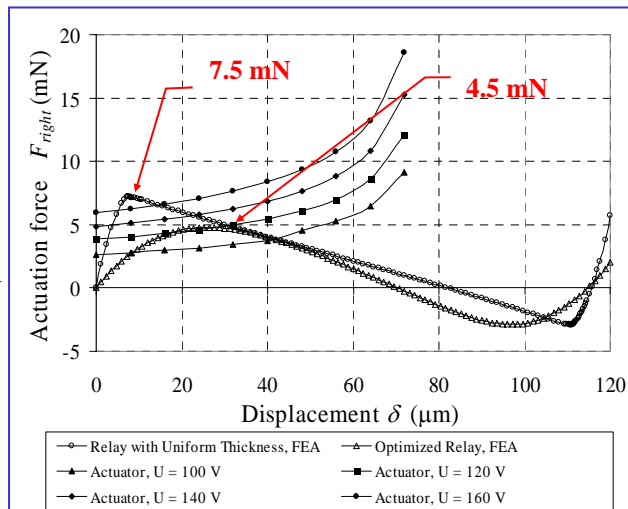


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Optimization of The Double Beam (II)



- Actuation force/Contact force ratio starts from $\sim 2.5:1$.
- Beam was modulated, force ratio was optimized to $\sim 1.5:1$.
- ~ 120 V is needed to actuate the relay.



Force-Displacement curves of the actuator and the double beam

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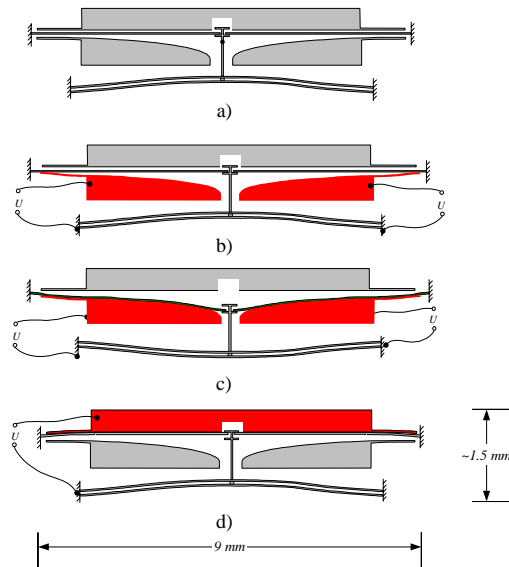
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The Relay



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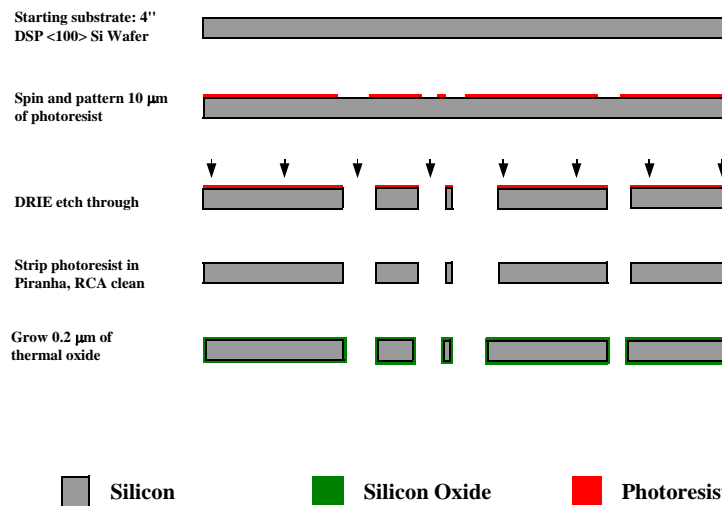
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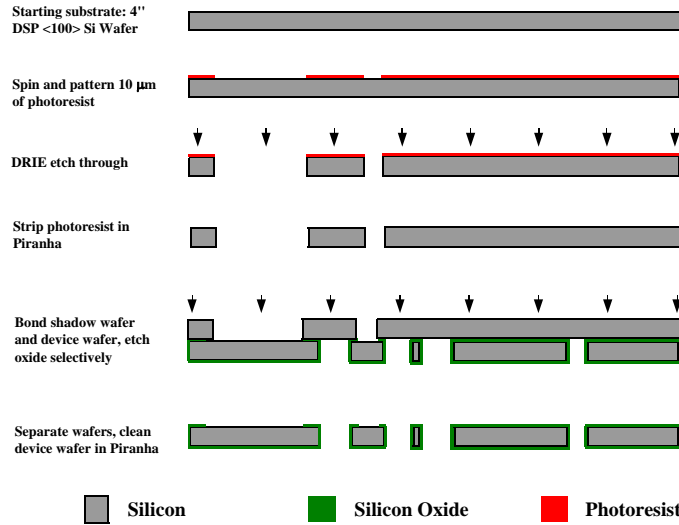
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Fabrication: Process Flow (1)



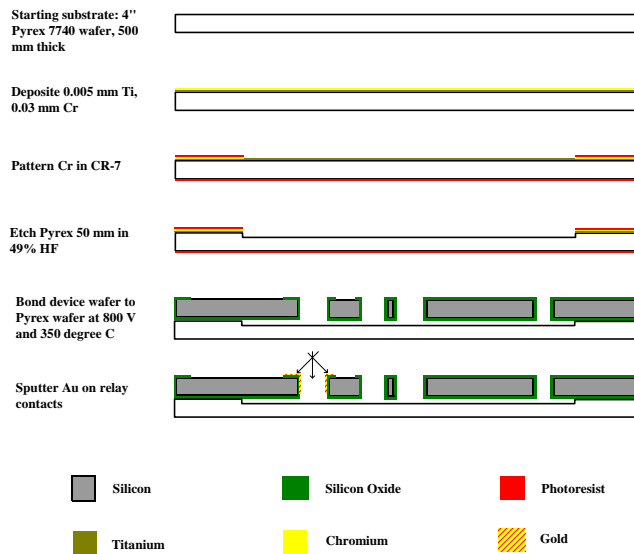
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Fabrication: Process Flow (2)



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Fabrication: Process Flow (3)

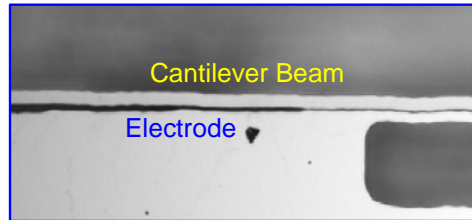


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Fabrication: Transparency Mask



- Transparency mask for device wafer:
 - Much faster and much cheaper
 - Low resolution: 3-4 μm
- Electrostatic force is very sensitive to the recess at electrode
- Print the mask 10 times larger and use 10:1 stepper to shrink it down



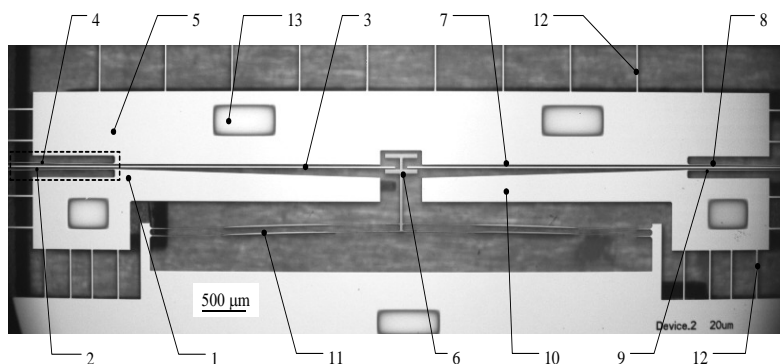
Device made using Transparency Mask



Device made using transparency mask and 10:1 Stepper

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Fabrication Results: Overview

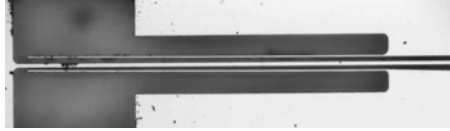


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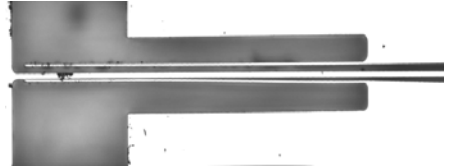
Measurement: Pull_in of the Starting Zone



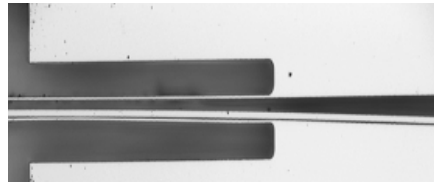
- The starting beam bends up and closes the gap between zipper beam and fixed electrode



- Pull-in at 75V

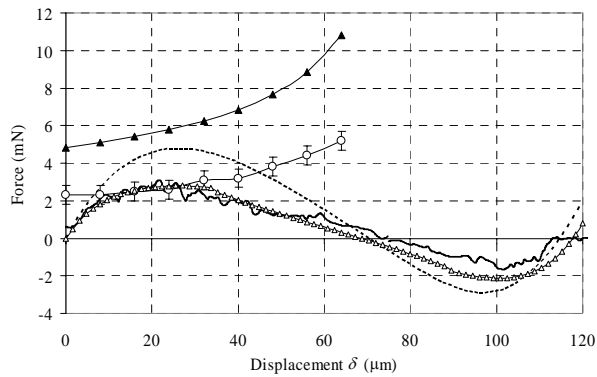


- 140 V. Zipper beam collapse to the fixed electrode, relay is closed



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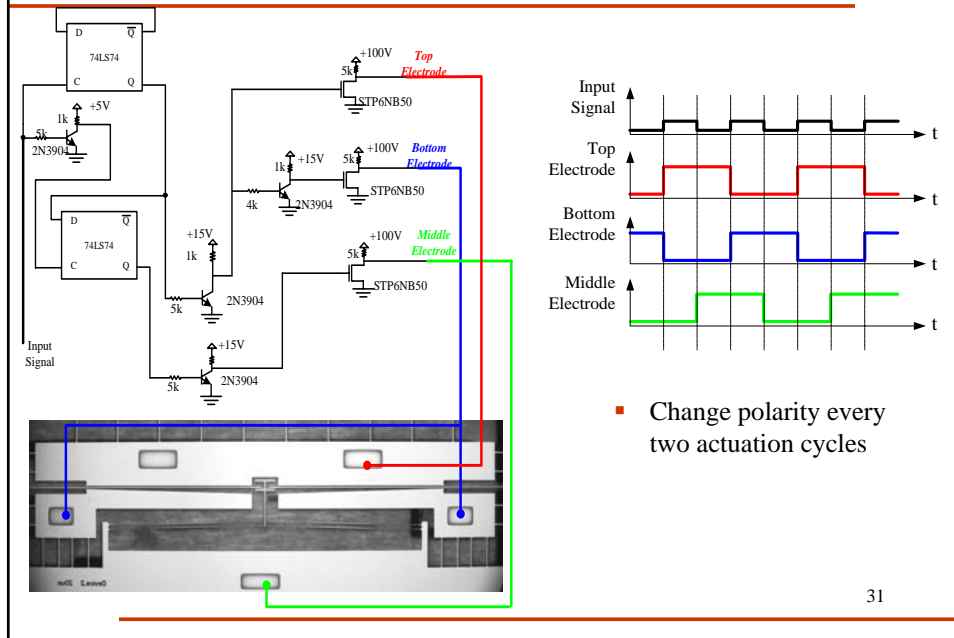
Force Measurement



Flextester

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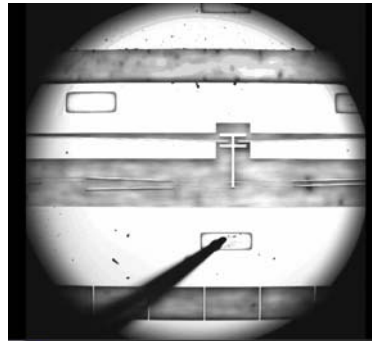
A Bipolar Drive to Avoid Stiction



Relay Actuated by Zipping Actuator

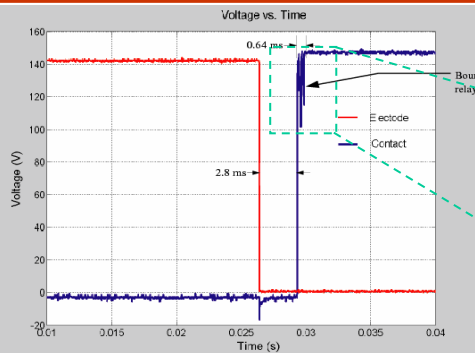


- > 40 millions of life cycles were achieved
- Maximum toggling speed: 160 Hz
- Shortest excitation pulse: 400 μ s



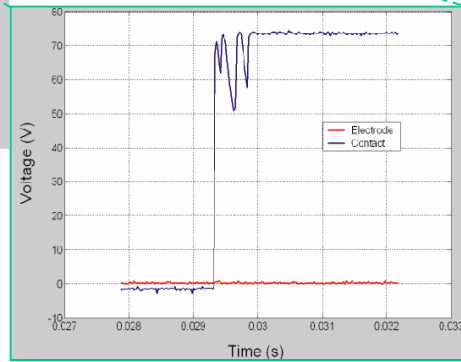
[Click for a movie](#)

Switching Time



- Contact bounce time ~ 0.5 ms

- Switching time ~ 3 ms



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Contributions



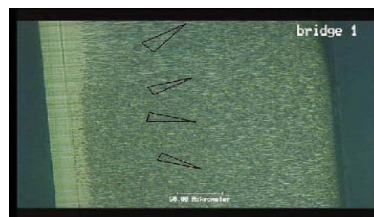
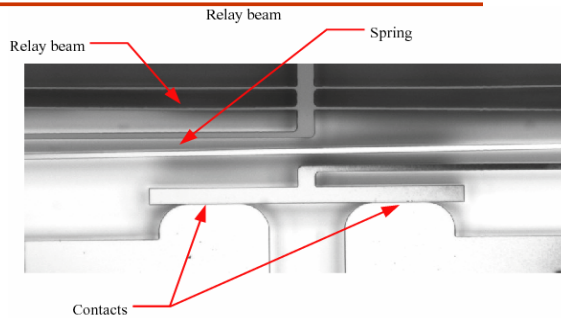
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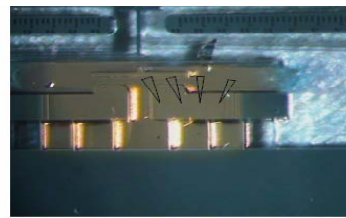
DRIE-etched Relay Contacts



- Relay contacts
- Vertical sidewalls
- Sputter Au: low efficiency.
- Sidewall/surface thickness ratio = 1/9
- Contact resistance:
~1 Ω



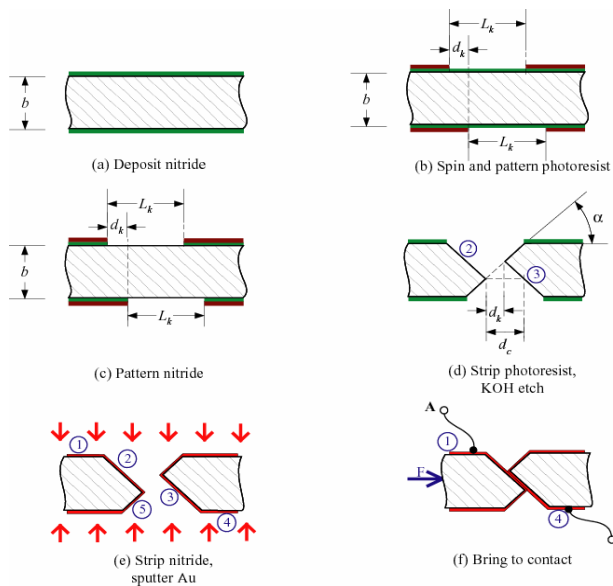
a)



b)

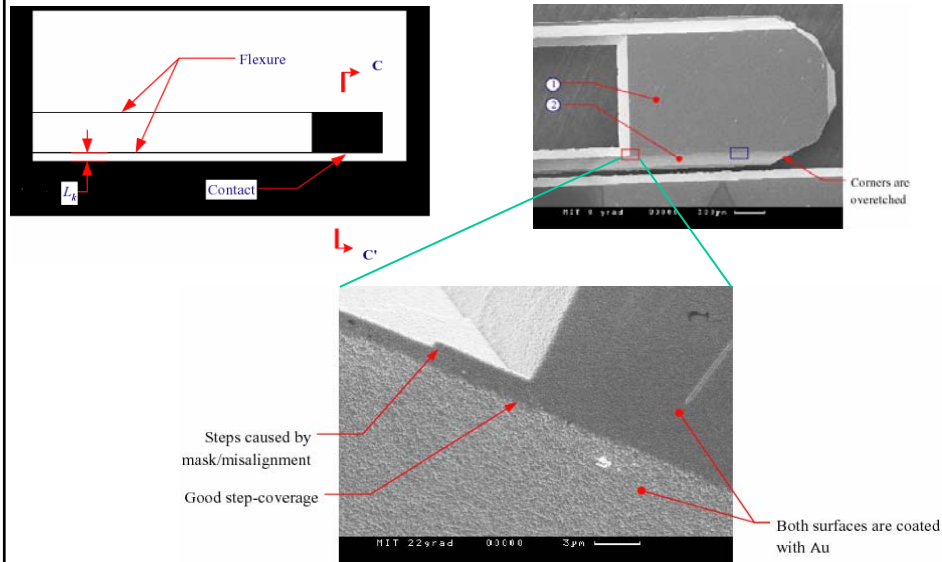
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KOH-etched Relay Contacts: Design



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KOH-etched Relay Contacts: Experiments

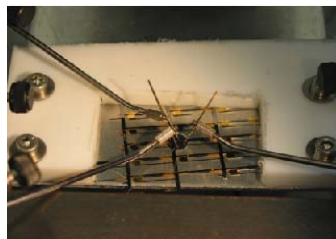


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KOH-etched Relay Contacts: Tests



- Sputter Au: high efficiency.
- Sidewall/surface thickness = 1/1.4
- Very low contact resistance: $\sim 50 \text{ m}\Omega$



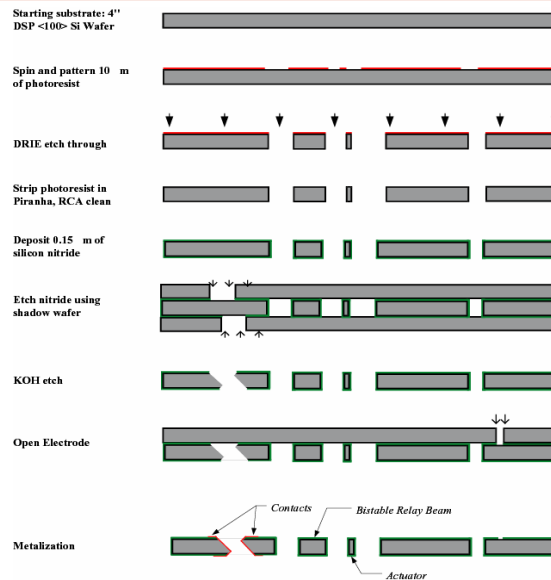
a)



b)

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Proposed Full Relay Process Flow



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Conclusions and Future Work



- **Conclusions:**
 - Design, modeling, optimization, fabrication and measurement of an actuator-relay system
 - Develop wet-anisotropically-etched relay contacts
- **Future work:**
 - Combine the actuator and the KOH-etched contacts
 - Vertically moving zipping actuators

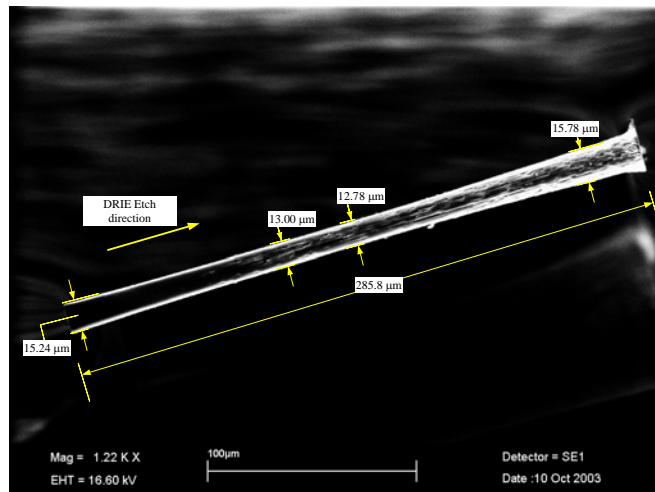
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Acknowledgements



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- *Discussion (PERG)*: Dr. Jin Qiu, Dr. Joachim Sihler
- *Fabrication (at MTL)*: Kurt Broderick, Dennis Ward, Paul Tierney, Linvhu Hol, Dr. Hongwei Sun ...
- *Testing (at ABB Research)*: Dr. Ralf Struempler, Dr. Sami Kotilainen, Dr. Jan-henning Fabian, Eric Wapelhorst, Jeff Renaud

Actuator Beam Profile



Optimization: Algorithm (1)



- Beam equation:

$$(EI w''')'' + T w'' = 0$$

$$(EI \delta w_i''')'' + T_i \delta w_i'' = -\delta T_i w_i'' - (E \delta I w_i''')''$$

- Fredholm alternative:

$$\int (\delta T_i w_i'' + (E \delta I w_i''')'') w_i dx = 0$$

$$\delta T_i = - \frac{\int w_i (E \delta I w_i''')'' dx}{\int w_i'' w_i dx} \quad \delta T_i = E \frac{\int \delta I (w_i'')^2 dx}{\int (w_i')^2 dx}$$

- Cost function variation:

$$\delta C(\{T_i\}) = \int \delta I \left[\sum_{i=1}^{\infty} \frac{dC}{dT_i} \frac{(w_i'')^2}{\int (w_i')^2} \right] = \int \delta I \Lambda(T_i, w_i)$$

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Optimization: Algorithm (2)



- Beam equation:

$$(EI (w - w_0)''')'' + \tau^2 w'' = f \delta(x - L/2)$$

- Transition state

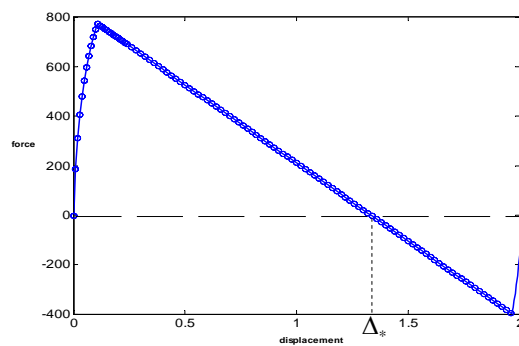
$$w_i = \Gamma w_0(x) + A w_n$$

$$\Gamma = (1 - (\tau/\tau_0)^2)^{-1}$$

$$\Delta_* = 1 - \Gamma$$

$$R = \frac{\Delta_*}{2 - \Delta_*} = \frac{(1 - \Gamma)}{2 - (1 - \Gamma)}$$

$$= \frac{(\tau_2/\tau_0)^2}{2 - (\tau_2/\tau_0)^2}$$



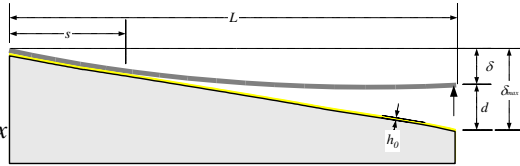
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Analytical Analysis (1)

- Beam equation:

$$EI\bar{y}''''(x) = p(x) = -\frac{\Gamma}{[\bar{y}(x) + \beta]^2} \Rightarrow$$

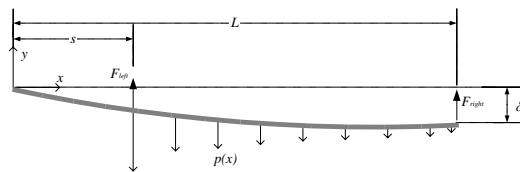
$$\Rightarrow \begin{cases} F_{left} = \frac{1}{L-s} \cdot \int_s^L -p(x) \cdot [(L-s) - x] dx \\ F_{right} = \frac{1}{L-s} \cdot \int_s^L p(x) \cdot (x-s) dx \end{cases}$$



- Near $x = s$

$$\bar{y}(x) = -\frac{\Gamma}{24EI\beta^2} (x-s)^4 + A(x-s)^3$$

$$\Rightarrow F_{left} = EI\bar{y}''''(s) = 6EIA$$



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Analytical Analysis (2)

- Assume most of the force comes from $s < x < x^*$

$$\begin{cases} F_{left} \sim \frac{1}{L-s} \cdot \int_s^{x^*} \frac{\Gamma}{\beta^2} \cdot [(L-s) - x] dx \sim \frac{\Gamma(x^* - s)}{\beta^2} \\ F_{right} \sim \frac{1}{L-s} \cdot \int_s^{x^*} p(x) \cdot (x-s) dx = \frac{\Gamma}{\beta^2} \frac{(x^* - s)^2}{L-s} \end{cases}$$

$$\left. \begin{aligned} \beta = \bar{y}(x^*) = A \cdot (x^* - s)^3 - \frac{\Gamma}{24EI\beta^2} (x^* - s)^4 \\ F_{left} = 6EIA \end{aligned} \right\} \Rightarrow \left. \begin{aligned} \beta \sim \frac{F_{left}}{6EI} \cdot (x^* - s)^3 - \frac{\Gamma}{24EI\beta^2} (x^* - s)^4 \\ F_{left} \sim \frac{\Gamma(x^* - s)}{\beta^2} \end{aligned} \right\} \Rightarrow$$

$$\Rightarrow \left. \begin{aligned} (x^* - s) \sim \left(\frac{EI\beta^3}{\Gamma} \right)^{1/4} \\ F_{right} \sim \frac{\Gamma}{\beta^2} \frac{(x^* - s)^2}{L-s} \end{aligned} \right\} \Rightarrow F_{right} \sim \frac{1}{L-s} \sqrt{\frac{EI\Gamma}{\beta}}$$

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Analytical Analysis (3)

Far from $x = s$

$$\left. \begin{aligned} \bar{y}(x) = B(x-s)^2 &\Rightarrow B \sim \frac{\Gamma}{2EI\beta^2}(x^*-s)^2 \\ (x^*-s) &\sim \left(\frac{EI\beta^3}{\Gamma}\right)^{1/4} \end{aligned} \right\} \Rightarrow \left. \begin{aligned} B &\sim \sqrt{\frac{\Gamma}{EI\beta}} \\ d = B(L-s)^2 & \end{aligned} \right\} \Rightarrow$$

$$\left. \begin{aligned} L-s &\sim \left(\frac{EI\beta}{\Gamma}\right)^{1/4} \sqrt{d} \\ F_{right} &\sim \frac{1}{L-s} \sqrt{\frac{EI\Gamma}{\beta}} \end{aligned} \right\} \Rightarrow F_{right} \sim \frac{1}{\sqrt{d}} (EI)^{1/4} \left(\frac{\Gamma}{\beta}\right)^{3/4} \Rightarrow F_{right} \sim \frac{E^{1/4} b}{\sqrt{d}} \left(\frac{\epsilon_0 \epsilon_r U^2 h}{h_0}\right)^{3/4}$$



Analytical Analysis (4)

